

the HE STEM Programme. Thanks to the many individuals who offered detailed advice. ©2010 - version draft 1, August 2010.

Stats & OR Network, the UK Physical Sciences Centres Academy Maths, and

Produced in conjunction with the Higher Education Academy Maths,

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The sample mean \bar{x} is an unbiased estimate of the population mean μ . The unbiased estimate of the variance of these n sample observations is $s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}$ which can be written as

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n x_i^2 - \frac{n\bar{x}^2}{n-1}$$

The sample unbiased estimate of standard deviation, s , is the

square root of the variance: $s = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}}$. The standard

deviation of the sample mean is called the standard error of the

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Product notation: $\prod_{i=1}^n x_i = x_1 \cdot x_2 \cdots x_n$.

Example: $\sum_{i=1}^5 i^2$ means $1^2 + 2^2 + 3^2 + 4^2 + 5^2$.

Instance: $\sum_{i=1}^3 x_i$ means $x_1 + x_2 + x_3$.

Note that it takes all whole number values from 1 to n . So, for

the sum $x_1 + x_2 + \cdots + x_n$ is written $\sum_{i=1}^n x_i$.

$a \leq b$ means a is less than or equal to b

$a < b$ means a is greater than b

Inequalities: $a > b$ means a is greater than b

$\log_{10} x = \frac{\ln x}{\ln 10}$.

Formula for change of base: $\log_a x = \frac{\log_b x}{\log_b a}$. Specifically,

$n \log_b A = \log_b A^n$, $\log_b 1 = 0$, $\log_b b = 1$.

$\log_b A + \log_b B = \log_b AB$, $\log_b A - \log_b B = \log_b \frac{A}{B}$.

Laws of Logarithms: for any positive base b , with $b \neq 1$,

$a \log_b x = \log_b (x^a)$. Equivalently, $\log_b x^a = a \log_b x$, where

$[H^+]$ = hydrogen ion concentration in mol dm⁻³ and

$pH = -\log_{10}([H^+]/c)$ so $[H^+] = 10^{-pH}$.

pH: of a solution to base 10. $\log_{10} A = c$ means $A = 10^c$.

Logarithms to base 10: $\log_{10} A = \ln(e_A) = A$.

e would have to be raised to equal A . Note:

c, the natural logarithm of a number A , is the power to which

$\log_e A$ or $\ln A = c$ means $A = e^c$.

start which is approximately 2.718.

Natural logarithms. The letter e denotes \log_e or alternatively ln are called

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