

# **Factorising simple expressions**

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#### Introduction

Before studying this material you must be familiar with the process of 'removing brackets' as outlined on leaflets  $Removing\ Brackets\ 1\ \&\ 2$ . This is because factorising can be thought of as reversing the process of removing brackets. When we factorise an expression it is written as a product of two or more terms, and these will normally involve brackets.

#### **Products and Factors**

To obtain the **product** of two numbers they are <u>multiplied</u> together. For example the product of 3 and 4 is  $3 \times 4$  which equals 12. The numbers which are multiplied together are called factors. We say that 3 and 4 are both factors of 12.

### **Example**

The product of x and y is xy.

The product of 5x and 3y is 15xy.

### **Example**

2x and 5y are factors of 10xy since when we multiply 2x by 5y we obtain 10xy.

(x+1) and (x+2) are factors of  $x^2+3x+2$  because when we multiply (x+1) by (x+2) we obtain  $x^2+3x+2$ .

3 and x-5 are factors of 3x-15 because

$$3(x-5) = 3x - 15$$

### **Common Factors**

Sometimes, if we study two expressions to find their factors, we might note that some of the factors are the same. These factors are called **common factors**.

### **Example**

Consider the numbers 18 and 12.

Both 6 and 3 are factors of 18 because  $6 \times 3 = 18$ .

Both 6 and 2 are factors of 12 because  $6 \times 2 = 12$ .

So, 18 and 12 share a common factor, namely 6.

In fact 18 and 12 share other common factors. Can you find them ?

### **Example**

The number 10 and the expression 15x share a common factor of 5.

Note that  $10 = 5 \times 2$ , and  $15x = 5 \times 3x$ . Hence 5 is a common factor.

# **Example**

 $3a^2$  and 5a share a common factor of a since

 $3a^2 = 3a \times a$  and  $5a = 5 \times a$ . Hence a is a common factor.

# **Example**

 $8x^2$  and 12x share a common factor of 4x since

 $8x^2 = 4x \times 2x$  and  $12x = 3 \times 4x$ . Hence 4x is a common factor.

# **Factorising**

To factorise an expression containing two or more terms it is necessary to look for factors which are common to the different terms. Once found, these common factors are written outside a bracketed term. It is ALWAYS possible to check your answers when you factorise by simply removing the brackets again, so you shouldn't get them wrong.

## **Example**

Factorise 15x + 10.

#### Solution

First we look for any factors which are common to both 15x and 10. The common factor here is 5. So the original expression can be written

$$15x + 10 = 5(3x) + 5(2)$$

which shows clearly the common factor. This common factor is written outside a bracketed term, the remaining quantities being placed inside the bracket:

$$15x + 10 = 5(3x + 2)$$

and the expression has been factorised. We say that the factors of 15x + 10 are 5 and 3x + 2. Your answer can be checked by removing the brackets again to show

$$5(3x+2) = 5(3x) + 5(2) = 15x + 10$$

2. 21 + 7x, 3. xy - 8x, 4. 4x - 8xy

#### **Exercises**

Factorise each of the following:

### Answers

1. 10x + 5y,

1. 
$$5(2x+y)$$
, 2.  $7(3+x)$ , 3.  $x(y-8)$ , 4.  $4x(1-2y)$ .