

# **Rearranging formulas 2**

mc-bus-formulas2-2009-1

#### Introduction

This leaflet develops the work started on leaflet *Rearranging Formulas 1*, and shows how more complicated formulas can be rearranged.

### **Further transposition**

Remember that when you are trying to rearrange, or **transpose**, a formula, the following operations are allowed.

- add or subtract the same quantity to or from both sides
- multiply or divide both sides by the same quantity

A further group of operations is also permissible.

A formula remains balanced if we perform the same operation to both sides of it. For example, we can square both sides, we can square-root both sides. We can find the logarithm of both sides. Study the following examples.

### **Example**

Transpose the formula  $p = \sqrt{q}$  to make q the subject.

#### Solution

Here we need to obtain q on its own. To do this we must find a way of removing the square root sign. This can be achieved by squaring both sides since

$$(\sqrt{q})^2 = q$$

So.

$$\begin{array}{rcl} p & = & \sqrt{q} \\ p^2 & = & q & \quad \text{by squaring both sides} \end{array}$$

Finally,  $q = p^2$ , and we have succeeded in making q the subject of the formula.

## **Example**

Transpose  $p = \sqrt{a+b}$  to make b the subject.

### Solution

$$\begin{array}{rcl} p & = & \sqrt{a+b} \\ p^2 & = & a+b & \text{by squaring both sides} \\ p^2-a & = & b \end{array}$$

Finally,  $b=p^2-a$ , and we have succeeded in making b the subject of the formula.

# **Example**

Make x the subject of the formula  $v = \frac{k}{\sqrt{x}}$ .

### Solution

$$\begin{array}{rcl} v & = & \frac{k}{\sqrt{x}} \\ v^2 & = & \frac{k^2}{x} & \text{by squaring both sides} \\ xv^2 & = & k^2 & \text{by multiplying both sides by } x \\ x & = & \frac{k^2}{v^2} & \text{by dividing both sides by } v^2 \end{array}$$

and we have succeeded in making x the subject of the formula.

## **Example**

Transpose the formula  $R = Q(1+i)^3$  for i.

### Solution

This must be carried out carefully, in stages, until we obtain i on its own.

$$R = Q(1+i)^3$$
 
$$\frac{R}{Q} = (1+i)^3$$
 by dividing both sides by  $Q$  
$$^3\sqrt{\frac{R}{Q}} = 1+i$$
 by taking the cube root of both sides 
$$i = \sqrt[3]{\frac{R}{Q}}-1$$
 by subtracting 1 from each side

### **Exercises**

- 1. Make r the subject of the formula  $V=\frac{4}{3}\pi r^3$ .
- 2. Make x the subject of the formula  $y = 4 x^2$ .
- 3. Make s the subject of the formula  $v^2 = u^2 + 2as$
- 4. Make P the subject of the formula  $S = P(1+i)^n$ . Try making i the subject.

#### **Answers**

1. 
$$r = \sqrt[3]{\frac{3V}{4\pi}}$$
. 2.  $x = \sqrt{4-y}$ . 3.  $s = \frac{v^2 - u^2}{2a}$ . 4.  $P = \frac{S}{(1+i)^n}$ .  $i = \sqrt[n]{\frac{S}{P}} - 1$